Power-Efficient Software Allocation in Wireless Sensor Networks

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Abstract

While designing the applicative domain of a Wireless Sensor Network, minimizing the energy consumption is crucial to maximize its overall lifetime. We propose a model and an heuristic for determining an optimal and fast sub-optimal functional allocation, guaranteeing applicative completeness and availability, under both functional and non-functional constraints.

ILP Model & Optimization Goal

We model a WSN as composed by:
• A set of N nodes \( N = \{ n_1, ..., n_N \} \)
• A set of F functions \( F = \{ f_1, ..., f_F \} \)

Functions may statically resides on the node memory or be dynamically loaded from the base station or the cluster head, to cope with memory bounds. Nodes and functions are characterized by the parameters listed in Table 1 and Table 2. Most real applications rely on a hierarchical routing tree with cluster-based topology.

We thus define:
• Clusters as partitions on the set of nodes
• Tasks as set of functions

The optimization goal can be expressed as:

\[
\min q \cdot \frac{E_{const,i}}{E_i} \quad \forall i \in \{1, N\}
\]

where:

\[
E_{const,i} = E_{sys,i} + E_{mem,i} + E_{dyn,i} + E_{route} + E_{obs,i}
\]

The contribution have the following meanings:
• \( E_{sys,i} \): Energy for running the functions statically or dynamically allocated to node \( i \).
• \( E_{mem,i} \): Energy for forwarding a dynamic function to node \( i \).
• \( E_{obs,i} \): Energy associated to neighboring nodes overhearing.

The output of the problem is described by the variables \( \phi_{ij} \) indicating the execution frequency of each function on node \( i \).

ILP Model Constraints

Several constraints need to be imposed for the model to be correct and significant.

First of all, the energy consumed by each node must not exceed the available energy:

\[
E_{const,i} \leq E_i
\]

To implement fault resilience we require that some functions are statically allocated with a minimum redundancy:

\[
\sum_{j=1}^{N} s_{ij} \geq R_j \quad \forall j \in \{1, F\}
\]

Memory constraints must also be met. This means that the sum of the size of all statically allocated functions and that of the biggest dynamically allocated function (in the pessimistic hypothesis of downloading each dynamic function on-the-fly) must not exceed the available memory:

\[
d_{ar} \cdot S_i + \sum_{j=1}^{F} s_{ij} \cdot S_j \leq M_i \quad \forall i \in \{1, N\}
\]

The completeness of the task is then required, to assure that all functions are allocated at least once, either statically or dynamically:

\[
\sum_{j=1}^{F} s_{ij} + d_{aj} \geq 1 \quad \forall j \in \{1, F\}
\]

Finally, some additional constraints are required to enforce non-negativity, frequency upper bounds, mutual exclusion between a static and a dynamic allocation of a given function, for each node:

\[
\sum_{j=1}^{F} \phi_{ij} \leq \phi_{i} \quad \forall j \in \{1, F\}
\]

Parameter Meaning

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>( d_{ar} )</td>
<td>Available memory</td>
</tr>
<tr>
<td>( E_i )</td>
<td>Energy capacity</td>
</tr>
<tr>
<td>( E_{sys,i} )</td>
<td>Energy consumed by OS and system functions</td>
</tr>
<tr>
<td>( H_i )</td>
<td>Set of successors in the routing tree</td>
</tr>
<tr>
<td>( N_i )</td>
<td>Set of neighboring nodes</td>
</tr>
</tbody>
</table>

Table 1: Node's parameters

Parameter Meaning

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>( S_i )</td>
<td>Energy footprint</td>
</tr>
<tr>
<td>( \phi_{i} )</td>
<td>Execution per hour</td>
</tr>
<tr>
<td>( E_{exec} )</td>
<td>Execution energy</td>
</tr>
<tr>
<td>( E_{load} )</td>
<td>Loading energy</td>
</tr>
<tr>
<td>( E_{trans} )</td>
<td>Transmission energy</td>
</tr>
<tr>
<td>( E_{recv} )</td>
<td>Reception energy</td>
</tr>
<tr>
<td>( R_i )</td>
<td>Minimum required redundancy</td>
</tr>
</tbody>
</table>

Table 2: Function’s parameters

Minimization Heuristic

Since the ILP problem often requires very long computation times, we have defined an heuristic algorithm for lifetime maximization under the constraints just described. It is outlined by the pseudo-code of Algorithm 1 and is structured into three steps:

1. Critical functions (\( R_i > 1 \)) first, the other next, are statically allotted to the nodes in a reverse and iterated breadth-first order on the routing tree. The remaining functions are finally allocated dynamically in top-down breadth-first order.

2. Multiple instances of each function are then allocated to nodes in order to scatter the execution frequencies among more nodes.

Results

A complete and integrated optimization flow has been implemented using GNU Octave, GLPSOL and custom tools developed on purpose. It is divided in three main phases:

1. Generation of random test instances
2. Execution of the ILP model solver and the heuristic algorithm
3. Verification of feasibility of the solution found

Test instances are generated drawing data from a real dataset, obtained in a previous work.

All the energy consumption parameters have been estimated combining the methodology in [1], with devices characterization figures found in [2]. The results obtained demonstrated very good results in balancing energy, since the gap between the node with more remaining energy and the one with less, is always less than 3% for the ILP model and under the 7% for the heuristic.

The heuristic, in particular, proved to be very fast and accurate if compared to the optimal solution:

• It runs 6 order of magnitude faster than ILP
• It produces results with a relative error less than 3.3% w.r.t. the ILP solution.

References
