A Fuzzy-C- Means Clustering Algorithm for a Volumetric Analysis of Paranasal Sinus and Nasal Cavity Cancers

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Abstract—In this paper, a semi-automatic segmentation algorithm for volumetric analysis of paranasal sinus and nasal cavity cancers is presented and validated. The algorithm, based on a semi-supervised Fuzzy-C-means method, was applied to a Magnetic Resonance data sets (each of them composed by T1-weighted, Contrast Enhanced T1-weighted and T2-weighted images) for a total of 64 tumor-contained slices. Method performances are tested by both a numerical and a clinical validation. Results show that the proposed method has a higher accuracy in quantifying lesion area than a Region Growing algorithm and it can be applied in the evaluation of tumor response to therapy.

I. INTRODUCTION

Paranasal sinus and nasal cavity cancers are pathologies that, after a radiotherapy treatment, may present a highly infiltrative growth pattern. In general the tumor volume cannot be easily assessed, because its irregular shape makes crude measurement difficult and limited in accuracy [1]. Often, clinicians must manually trace lesion outlines and this entails a lot of time.

Literature shows a lack of quantitative methods for paranasal sinus and nasal cavity cancers volume analysis using Magnetic Resonance Imaging (MRI) principally for the following reasons [1][2][3][4]: (1) the infiltrative growth pattern and irregular shape of tumor, (2) the complexity of neighbor anatomical tissues, usually with similar pixel intensity distribution, (3) tumor pixel intensity is often inhomogeneous, (4) partial volume effect makes lesion outlines blurred.

Classical algorithms [2] used for medical images segmentation are based on thresholding, clustering, region growing and contour extraction. Among these, clustering is the most suitable technique for our purposes, because it permits to combine information from a set of different images even if outlines are not well-visible [2][4]. In particular, a Fuzzy approach [4][5] may take into account the uncertainty in attributing a pixel to a given class of tissue.

Bear in mind these facts, we implemented a semi-automatic method to segment paranasal sinus and nasal cavity cancers for volume analysis. Information for the segmentation process is obtained through a weighted composition of three different MR images (T1-weighted, Contrast Enhanced T1-weighted and T2-weighted images) and segmentation is based on a supervised Fuzzy-C-means (SFCM) algorithm.

The method was tested on 64 tumor-contained slices through two types of validation: i) a numerical validation in which segmentation outcomes obtained by SFCM were compared with manual segmentation performed by an experienced radiologist and ii) a more qualitative validation in which clinician criteria (including the erroneous involvement of essential anatomical structures) were considered. A comparison with Region Growing based algorithm [5] was carried out.

II. MATERIALS AND METHODS

A. Experimental Protocol and Image Acquisition

The algorithm was tested in an experimental protocol developed at the Department of Images for Diagnosis and Therapy of the National Cancer Institute of Milan. We analysed 6 patients for a total of 10 exams. All patients underwent 1.5 T MR imaging (Siemens Vision, Erlangen). Spin-echo and turbo-spin-echo sequences were used to obtain T1-weighted (T1), contrast-enhanced T1-weighted (Gadolinium, Gd-T1), T2-weighted (T2) images. The 512X512 pixel images of the head in the axial plane were acquired with a 4096 (12 bits) greyscale, slice number of 18-21, slice thickness of 5 mm and slice gap of 1 mm. A total number of 64 tumor-contained slices were considered.

B. Semi-supervised fuzzy-C-method

Semi-supervised methods use a small amount of labeled data as a guide to unsupervised techniques. This may be useful especially in difficult and noisy tasks where little a
priori information is available, such as for brain tumor segmentation [4]. In our approach the a priori information is obtained through an automatic clusters initialization and through a selection (made by the radiologist) of a few seed pixels belonging to tumor.

Let \( n \) be the number of pixels of a slice containing tumor, \( X = \{ x_1, \ldots, x_n \} \) is the set of the MR image data, where \( x_k = (\omega_{T1X_{T1}}, \omega_{Gd-T1X_{Gd-T1}}, \omega_{T2X_{T2}}) \), and where \( 1 \leq k \leq n \), \( \omega_{T1} \), \( \omega_{Gd-T1} \), \( \omega_{T2} \) are factors weighting the contribute of T1-weighted, Contrast Enhanced T1-weighted and T2-weighted image in the clustering procedure, respectively. Let \( C \) be the image clusters number, for each data, a “fuzzy” membership [6][7], \( u(x_k) = [u_{1k}, u_{2k}, \ldots, u_{Ck}] \) is computed. Each \( u_{ik} \) (\( 1 \leq i \leq C \)), has a value between 0 and 1, and \( \sum_{i=1}^{C} u_{ik} = 1 \). A matrix \( U \), consisting of \( C \times n \) elements, is defined by combining the \( u(x_k) \) of each pixel.

The inclusion of a priori knowledge of known membership is obtained by partitioning the \( X \) data matrix in this way:

\[
X = [X^l | X^u]
\]

where \( X^l \) is the labeled and \( X^u \) is the unlabeled part of the data, respectively. Accordingly, the initial \( U \) matrix is formed by \( n_l \) columns of labeled pixel vectors having crisp membership (1 or 0) and \( n-n_l \) columns of unlabeled pixel vectors whose values must be determined.

To find the values of unlabeled columns of the \( U \) matrix the following function is minimized [4]:

\[
J_m = \sum_{i=1}^{C} \sum_{k=1}^{N} u_{ik}^m \left\| X_k - V_i \right\|^2, 1 \leq m \leq \infty
\]

where \( V_i = [V_1, \ldots, V_C] \) are the cluster centers and \( m \) is the fuzzification coefficient. Let \( m=2 \), the objective function leads to the minimal square errors of the estimated membership matrix [5].

The first time the \( V_i \) are defined considering only the \( X^l \) data, while for the \( u_{ik} \) updating only \( X^u \) are taking into account.

The process ends when the error (distance between the new and old unlabeled columns of the \( U \) matrices) is smaller than a threshold or after a maximum number of iterations.

For our application, different settings (i.e. number of clusters and different combination of image features) were evaluated. The optimal selection algorithm of parameters was obtained using 8 clusters and setting \( \omega_{T1}=0.5, \omega_{Gd-T1}=1, \omega_{T2}=0.1 \).

### C. Segmentation algorithm

The segmentation procedure is shown in Fig. 1. It is applied for any slice containing a tumor.

First of all, the radiologist selects one or more (if inhomogeneous) pixels belonging to tumor tissues. This is important for the successive selection of the Region of Interest (ROI) containing tumor.

Next, the initial guess for SFCM algorithm is obtained by an automatic clusters initialization. This is realized considering the bidimensional histogram formed by T1-weighted and Contrast Enhanced T1-weighted images (Fig. 2). In this histogram the different tissues (air, spinal cord, normal tissues, mucosa and soft palate, tumor, fat) are mapped in different histogram areas where there are local maxima. Cluster centers are initialized by local maxima intensity values in the selected areas. The “tumor cluster” is initialized directly by the radiologist.

When SFCM ends, the defuzzification operation permits to assign a label to any image pixel. Then, the segmented tumor is refined using erosion and dilatation operations in order to obtain a more accurate lesion mask [4]. Finally, the mask is superimposed on the image (see Fig. 4).

### D. Validation procedure

For evaluating algorithm performances two types of validation were used. First, a numerical validation was used to compare our algorithm with a Region Growing algorithm and to quantify accuracy of the segmentation method. Then, a qualitative validation was used to evaluate the clinical usefulness of the our method.
Numerical validation.
An experienced radiologist manually segmented all 64 tumors contained in our dataset (Ground Truth, GT). Two indices were calculated [4]:

- percent match: \( PM[\%] = \frac{TP}{GT} \times 100 \);
- positive prediction value: \( P + [\%] = \frac{TP}{TP + 0.5 \cdot FP} \times 100 \);

where \( TP \) = true positives and \( FP \) = false positives. (See Fig. 3 for definition of \( TP \) and \( FP \)).

Clinical validation
An experienced radiologist scored FCM and RG segmented tumor on the basis of three criteria:

1. no involvement of essential anatomical structures (i.e. optic nerve) in the tumor area.
2. no volume errors (underestimation or overestimation) that may lead to errors in treatment planning.
3. correspondence with GT.

For each segmented tumor, the radiologist checked which criteria were satisfied.

III. RESULTS

The algorithm was compared with a Region Growing (RG) algorithm [5].

An example of segmentation obtained by the two methods is shown in Fig. 4, were tumor masks were positioned on the T1-Gd image. In the original T1-Gd image, it can be noted the tumor infiltrations and the similarity of grey-levels between tumor pixels and the neighbours ones. In this case, both SFCM and RG seem to show a good performance, but using RG, a GT underestimation is present.

Table 1 reported a comparison of PM and \( P + \) values in the case of RG, SFCM using only two images (T1-w and T1) without weighted factors as in [4] (SFCM2) and our algorithm (SFCM):

<table>
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<th></th>
<th>RG</th>
<th>SFCM2</th>
<th>SFCM</th>
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<tr>
<td>PM(%)</td>
<td>66.26</td>
<td>74.09</td>
<td>74.65</td>
</tr>
<tr>
<td>( P + ) (%)</td>
<td>82.01</td>
<td>81.21</td>
<td>89.89</td>
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We may observe that both PM and \( P + \) increase using SFCM algorithm. In particular, \( P + \) value indicates that our algorithm is able to correctly estimate tumor size and location.

Table 2 shows the percentage of analyzed cases in which results satisfied the clinical criteria.

Even if the three clinical criteria were better followed by SFCM, there is still the possibility to erroneously attribute important anatomical structures to tumor area.

Fig. 4: Comparison between SFCM and RG outcomes with respect to GT. Masks (in red) are overlapped on the T1-Gd original image (at left).
In Fig. 5 an example of erroneous involvement of essential anatomical structures is presented. It can be noted that, in both methods, the optical nerve is included. However, in this case the error is prominent using RG, in fact two optical nerves are included and the true tumor volume is underestimated.

IV. DISCUSSION AND CONCLUSION

In this work, our method was compared to Region Growing: both numerical results and clinical validation show the better performance of our method, which appears to be enough accurate to evaluate the tumor response to therapy [8]. For other applications in which a more high accuracy is requested, such as radiotherapy and surgery treatment planning, the use of this method is not yet advisable.

REFERENCES